

TURAN, Gyorgy

Central control reading of kilowatt-hour meters. Villamosság 8  
no.11:347 N '60.

1. "Villamosság" szerkesztoje.

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"Lighting of the Kansas City railroad yard." Reviewed by Gyorgy  
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Formation of household current consumption in the United States.  
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1. "Villamossag" szerkesztoje.

TURAN, Gyorgy

Some words on the necessity of using the electro-stimulator.  
Villamossag 9 no.12:378 D '61.

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"Starting, change of revolution number, and braking of asynchronous motors" by Dr. Laszlo Kovacs. Reviewed by Gyorgy Turan. Villamossag 10 no.5:153 My '62.

1. "Villamossag" szerkesztoje.

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Letter to the editor. Villamosag 10 no.6:184 Je '62.

1. "Villamosag" szerkesztoje.

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"Low voltage switching devices" by Bela Medek. Reviewed by Gyorgy Turan.  
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Congress of the Polish Electrotechnical Association held in Gleiwitz. p.90.

VILLAMOSSAC. Budapest, Hungary. Vol. 7, no. 3, Mar. 1959.

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Uncl.



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Experimental stereophonic radio broadcasting in Europe. Villamossag 12 no.5:159 My '64.

1. Editor, "Villamossag."

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Installation of a multiple condenser battery in Szombathely. p.92.

VILLAMOSSAG. Budapest, Hungary. Vol. 7, no. 3, Mar. 1959

Monthly List of East European Accessions (EEAI), LC. Vol. 8, No. 9, September 1959  
Uncl.

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TURAN, GY. New possibilities for reviving victims of accidents with electricity. p. 215.

Vol. 4, No. 7, July 1956.

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TECHNOLOGY

Budapest, Hungary

So: East European Accession, Vol. 6, No. 2, Feb. 1957

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More attention is needed in connecting repaired implements. p. 94.  
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SO: Monthly List of East European Accessions (EEAL) LC, Vol. 6, no. 6, June 1957. Uncl.

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Phase correction of portal cranes.

P. 145. (Villamossag. Vol. 5, no. 4/5 July/Aug. 1957, Budapest, Hungary)

Monthly Index of East European Accessions (EFAI) LC. Vol. 7, no. 2,  
February 1958

TURAN, GY.

Equipment for phase correction made from condensers of metallic paper based on prefabricated elements.

P. 145 (Villamossag. Vol. 5, no. 4/5 July/Aug. 1957, Budapest, Hungary)

Monthly Index of East European Accessions (EEAI) LC. Vol. 7, no. 2,  
February 1958

TURAN, GY.

Application of parallel condensers in medium and high-voltage networks.

p. 146 (Villamossag. Vol. 5, no. 4/5 July/Aug. 1957, Budapest, Hungary)

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February 1958



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TURAN, GY. Janos Endrenyi and Dezso Devenyi's Erintesvedelem (Protection against Shock);  
a book review. p. 223.

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Natural power factor, p. 206, MAGYAR ENERGIAGAZDASAG, (Energiagaz-  
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SOURCE: East European Accessions List (EEAL) Library of Congress,  
Vol. 5, No. 11, November 1956

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A highly significant step in the field of illuminating engineering: development of more economic light sources in line with the most recent achievements in colorifics. Villamossag ll no.12:377-378 D'63.

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"Correlation between the level of exposure and visibility."  
Reviewed by Gyorgy Turan. Villamossag 11 no.5:154 My '63.

1. "Villamossag" szerkesztoje.

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The direct-current series system of distribution built at  
Ikervar in 1896. Elektrotechnika 56 no.5:215-226 My '63.

1. Orszagos Villamosenergia Felugyelet osztalyvezetoje,  
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TURAN, Gy.

"Installation with Combined Switching, Protecting, Signaling, and Discharging for Phase-correcting Condensers", P. 124, (VILLANOVASAG, Vol. 5, No. 4, April 1954, Budapest, Hungary)

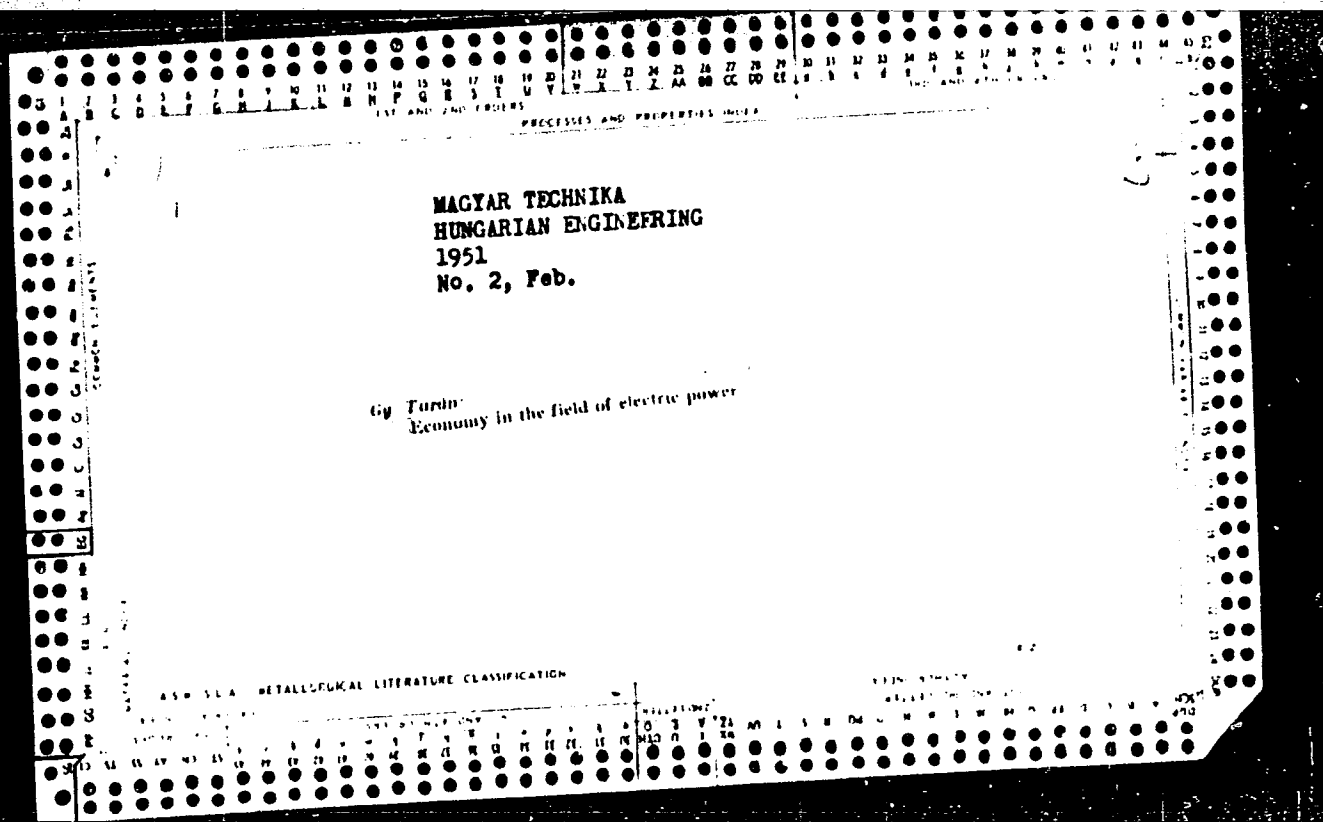
SC: Monthly List of East European Accessions (FEAL), LC, Vol. 4, No. 3, March 1955, Uncl.

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Questions relating to the technical development and economy of  
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1. Orszagos Villamosenergia Felugyelet osztalyvezetoje.

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(Electric machines)





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"Utilization of Soviet experiences in the flight and electric accidents". p. 111,  
(ELEKTROTEKHNIKA, Vol. 16, no. 6, June 1953, Budapest, Hungary)

SC: Monthly List of East European Accessions, L.G., Vol. 2, No. 11, Nov. 1953, Incl.

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"Remarks on Gyorgy Farago's article 'The Calculation, Maintenance, and Economy of Luminous Tube Lighting'", p. 92, (ELEKTROTECHNIKA, Vol. 16, no. 3, March 1953, Budapest, Hungary)

SO: Monthly List of East European Accessions, L.C., Vol2, No. 11, Nov. 1953, Uncl.

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Lighting of foundries. Villamossag 9 no.3:242-248 Ag '61.

1. Orszagos Villamosenergia Felugyelet.

TURAN, Gyorgy

Adequate use of electric motors. Villamossag 10 no.2:57-58 P '62.

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"Technical and economical aspects of keeping cables with 5, and 6 kV nominal voltage in 10 kV operation." Reviewed by Gyorgy Turan. Villamosság 8 no.4:122 Ap '60.

1. "Villamosság" szerkesztoje.

OSZTROVSZKY, Gyorgy; Schiller, Janos; PALFI, Laszlo, okleveles villamosmernok;  
BOZSIK, Ferenc; GYORI, Attila, okleveles villamosmernok, foenergetikus;  
VARGA, Endre, okleveles gepeszmernok; TURAN, Gyorgy, okleveles gepesz-  
mernok; SZENDY, Karoly, dr., fokonstruktor; KOVACS, Ferenc, okleveles  
villamosmernok; CSILY, Jenő, fodiszpecser; BEREZNAV, Frigyes, fomer-  
nok; PALOS, Ferenc, okleveles mernok; FILARSZKY, Zoltan, okleveles  
gepeszmernok; NEMETH, Imre, okleveles villamosmernok, fomernok; AL-  
PAR, Imre, okleveles gepeszmernok, foenergetikus; GATI, Geza, okle-  
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SZKY, Endre, foeloado; VERKITS, Gyorgy, okleveles villamosmernok, fo-  
mernok; FUTO, Istvan, oklevels gepeszmernok; NAGY, Karoly; PIKLER,  
Ferenc; SZEPESSY, Sandor, okleveles gepeszmernok; NADAY, Zoltan, ok-  
leveles gepeszmernok, fotechnologus; BUCHHOLCZ, Janos, okleveles ge-  
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An account of the 11th itinerant meeting of the Hungarian Electro-  
technical Association held in Pecs, July 18-20, 1963. Energia es atom  
16 no.12:559 D '63.

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"Practical experiences with the iodine charged new light sources with quartz bulbs." Reviewed by Gyorgy Turan. Villamossag 8 no.4:123 Ap '60.

1. "Villamossag" szerkeszto bizottsagi tagja.

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"High lumen maintenance and easy starting of mercury lamps" by  
E. C. Wartt, K. Gottschalk and A.C. Green. Reviewed by Gyorgy  
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1. "Villamossag" szerkesztoje.



TURAN, Gyorgy

Preventing injuries from electricity. Villamossag 8 no.4:123  
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1. "Villamossag" szerkesztoje.

TURAN, Gyorgy

The stimulator has again saved a life! Workshop experiences.  
Villamossag 11 no.8:255-256 Ag '63.

1. "Villamossag" szerkesztoje.

TURAN, Gyorgy

Start of single-phase supplied asynchronous motors. Villamossag  
II no.7:214-216 JI '63.

1. "Villamossag" szerkesztoje.

CSASZAR, Akos; FRIED, Ervin; FUCHS, Laszlo; HAJOS, Gyorgy; RENYI, Alfred;  
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Report on the 1962 Miklos Schweitzer Memorial Contest on  
Mathematics. Mat lapok 14 no. 3/4:346-371 '63.

1. Editorial board member. "Matematikai Lapok" (for Hajos and  
Renyi). 2. Managing editor. "Matematikai Lapok" (for Turan).

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14 no. 3/4:264-275 '63.

1. Managing editor, "Matematikai Lapok."

SZUSZ, Peter, a matematikai tudományok doktora; KADOC, P.; FENYI, Alfred;  
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Contribution to the metric theory of continued fractions. Ma- kozl  
MTA 14 no.4:361-400 '64.

1. Editorial Board Member, "A Magyar Tudományok Akadémiá Matematikai  
és Fizikai Tudományok Osztályának Közleményei" (For Rényi and Turan).

BALAZS, J.(Budapest); TURAN, Pal, Member, Hungarian Academy of Sciences(Budapest)

Notes on interpolation. VIII. (Mean convergence in infinite intervals).  
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1. Editorial Board Member, "Acta Mathematica Academiae Scientiarum  
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"APPROVED FOR RELEASE: 03/14/2001

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KNAPOWSKI, S. (Poznan); TURAN, P. (Budapest)

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Assuming that  $\phi(x) = 0$  for  $x \geq 0$ , we have for the rest,

$$|f_n| \leq 2^{3/2} (1 + |x_n|^{-1/2})$$

(over)

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$$E' = \max_{0 \leq \mu \leq (1/n - 1)} \{ \dots \}^{1/2} (n-1),$$

$0 \leq \mu \leq (1/n - 1).$  Further results deal with conditions on the ,  
coefficients involving the reality of all zeros. For instance,

TURÁN, PAUL

Mathematical Reviews  
Vol. 14 No. 8  
Sept. 1953  
Analysis

8-10-54  
LL

Turán, Paul. On a property of lacunary power-series.

Acta Sci. Math. Szeged 14, 209-218 (1952).

The paper contains results on entire functions

$$f(z) = \sum_{n=0}^{\infty} a_n z^{\lambda_n}$$

with Fabry gaps ( $n/\lambda_n \rightarrow 0$ ) related to those of Pólya and Sunyer i Balaguer [cf. Sunyer i Balaguer, Collectanea Math. 2, 129-174 (1949); these Rev. 12, 489]. For such functions and sufficiently large  $r$  the inequality

$$M(r)^{1+\alpha} \leq \{48\pi/(\beta-\alpha)\} M(2r) M(r, \alpha, \beta)$$

is established where  $M(r, \alpha, \beta)$  is the maximum modulus of  $f(z)$  on  $|z|=r$  with  $\alpha \leq \arg z \leq \beta$  and  $M(r) = M(r, 0, 2\pi)$ . A similar result for harmonic functions with lacunary Fourier series is obtained. The proof is novel and "elementary", exploiting an inequality previously given by the same author [these Rev. 9, 80].

A. J. Macintyre.

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Maximal order of the element  $\nu$  in  $G$  consists of proving the first statement. The difficult "second problem" deals with the case  $m \geq 0$ . The results are as follows. If  $m \geq 0$ , then (i) there is an integer  $\nu$  ( $m \leq \nu \leq m+k$ ) such that

$$|f(\nu)| \nu^{-\nu} \geq k^k (2e(m+k))^{-k} |a_1 + \dots + a_k|;$$

and (iii) if, moreover,  $U = |z_1| \geq \dots \geq |z_k|$  then there is also a  $\nu$  ( $m \leq \nu \leq m+k$ ) such that

$$|f(\nu)| \nu^{-\nu} \geq k^k (2e(m+k))^{-k} \min_{1 \leq i \leq k} |z_i + \dots + z_k|.$$

Part II. §1 and §2. Generalization of inequalities of Littlewood [see Theorem 1.1 and 1.2]. See also [1047].

[illegible]

Mathematical Reviews  
Vol. 14, No. 11  
Dec. 1953  
Analysis

✓ Turán, P. On a trigonometrical sum. *Ann. Soc. Polon. Math.* 25 (1952), 155-161 (1953).

The author gives two general theorems (the first is a corollary of the second), each of which contains the positivity of the sums (1)  $\sum_{v=1}^n v^{-1} \sin vx$  on  $(0, \pi)$ . (1) If  $\sum_{v=1}^n b_v \sin (2v-1)x > 0$  on  $(0, \pi)$ , then  $\sum_{v=1}^n v^{-1} b_v \sin vx > 0$  also. (11) If  $a_v$  are real numbers such that

$$(2) \quad f(x) = \sum_{v=0}^n a_v \cos vx \geq 0 \quad \text{and} \quad \sum_{v=1}^n a_v = 0,$$

then (3)  $\sum_{v=1}^n v^{-1} (a_0 + a_1 + \dots + a_{v-1}) \sin vx > 0$  on  $(0, \pi)$ . Theorem II is proved by a complex-variable method similar to that used by the author for (1) [*J. London Math. Soc.* 13, 278-282 (1938)]. Other results are that for  $0 < x < \pi$  and  $n \geq 2$ ,

$$\sum_{v=1}^n v^{-1} \sin vx > 4 \sin^2 \frac{1}{2} x \left\{ \tan \frac{\pi-x}{2} - \frac{\pi-x}{2} \right\};$$

that if  $\sum a_v = 0$  and  $f(x)$  in (2) satisfies  $|f(x)| \leq M$ , then  $g(x)$  in (3) satisfies  $|g(x)| \leq M(\pi-x)/2$ ; and that if  $f(\theta) = \sum b_v \sin v\theta$  is odd in  $(0, 2\pi)$ , convex in  $(0, \pi)$ , and  $f(r, \theta) = \sum b_v r^v \sin v\theta$  is the corresponding harmonic function, then  $\sum_{v=1}^n v^{-1} b_v r^v \sin v\theta \geq 2f(r, \theta)$  in the upper half of the unit circle.

R. P. BOAS, JR. (Evanston, Ill.).

TURÁN, PÁL

✓ Turán, Pál. Some remarks on theory of functions and theory of series. Eötvös L. Tud.-Egy. Kiadv. Term. Tud. Kar Evk. 1952-53, 5-13 (1954). (Hungarian) 1 - F/W

The author discusses various problems and results on the theory of functions and summability. Among others he proves the following theorem. Let  $\alpha$  be a complex number with  $\Im(\alpha) \neq 0$ ; then there exists an analytic function  $f(z) = \sum_{n=0}^{\infty} a_n z^n$  whose only singular point is at  $z=1$ , and for which

$$(*) \quad \sum_{n=0}^{\infty} \frac{f^{(n)}(\alpha)}{n!} (1-\alpha)^n$$

diverges (i.e. the Taylor expansion around  $\alpha$  diverges at  $1-\alpha$ ). The author shows that  $f(z) = e^{1/(1-z)}$  has the required property. He further asks if such an  $f(z)$  exists if  $-1 < \alpha < 0$ ? He remarks that if  $0 < \alpha < 1$  then by a theorem of Hardy and Littlewood (\*) converges (here we only have to assume that  $f(z)$  is analytic for  $|z| < 1$ )

P. Erdős (Haifa).





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Turán, Pál. The life and mathematics of Pál Turán. 1. 1990

TURÁN, P.

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Erdős, P., and Turán, P. On the role of the Lebesgue functions in the theory of the Lagrange interpolation. Acta Math. Acad. Sci. Hungar. 6, 47-66 (1955). (Russian summary)

1 = F/W

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Let  $A = (x_{vn})$  ( $v=1, 2, \dots, n; n=1, 2, \dots$ ) be a triangular matrix of interpolation points where  $-1 \leq x_{vn} \leq 1$  and all  $x_{vn}$  in one row are distinct. Let  $f(x)$  be continuous; we form the polynomials

✓

$$L_n(f) = \sum_{v=1}^n f(x_{vn}) l_{vn}(x),$$

where  $l_{vn}(x)$  denote the fundamental polynomials of the Lagrange interpolation. The authors investigate the following important class  $A(\beta)$  of matrices  $A$ . There exists a number  $\beta$ ,  $0 < \beta < 1$ , such that for the "Lebesgue constants"  $M_n = \max_{-1 \leq x \leq 1} |l_{vn}(x)|$  the following inequalities hold:

$$\limsup_{n \rightarrow \infty} M_n n^{-\beta-\epsilon} < c_1(\epsilon), \quad \limsup_{n \rightarrow \infty} M_n n^{-\beta+\epsilon} > c_2(\epsilon),$$

(over)

(1)

Erdős P. and Turán P.

where  $c_1(\epsilon)$ ,  $c_2(\epsilon)$  are positive constants. The following results are obtained. (a) Let  $\mu < \beta/(\beta+2)$ ; there exists an  $f(x) \in \text{Lip } \gamma$  such that  $L_n(f)$  is unbounded in  $[-1, 1]$  as  $n \rightarrow \infty$ . (b) Let  $\gamma > \beta$ ,  $f(x) \in \text{Lip } \gamma$ ; then the sequence  $L_n(f)$  is uniformly convergent in  $[-1, 1]$ . (c) Let  $\gamma > \beta/(\beta+2)$ ; there exists a special matrix  $A \in A(\beta)$  such that the corresponding  $L_n(f)$  converge uniformly in  $[-1, 1]$  whenever  $f(x) \in \text{Lip } \gamma$ . (d) Let  $\gamma < \beta$ ; there exists a special matrix  $A \in A(\beta)$  and a special  $f(x) \in \text{Lip } \gamma$  such that  $L_n(f)$  is unbounded in  $[-1, 1]$ . G. Szegő (Stanford, Calif.).

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TURAN, P. -matematikai Lapok-Vol. 6, no. 1, 1955.

Tenth Anniversary of our liberation. p. 1.

Life and mathematical work of Geza Grunwald. p. 6

SO: Monthly list of East European Accessions, (EEAL), LC, Vol. 4, No. 9, Sept. 1955  
Uncl.



TURAN, P.

On some new theorems in the theory of diophantine approximations. p. 241  
Vol. 6, no. 3/4, 1955

so. EAST EUROPEAN ACCESSIONS LIST Vol. 5, no. 7, July 1956

TURAN, P.

On the instability of systems of differential equations. In English. p. 257  
Vol. 6, no. 3/4, 1955

so. EAST EUROPEAN ACCESSIONS LIST Vol. 5, no. 7, July 1956

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TURAN, P.

TURAN, P. Distribution of "digits" of the "factorial" numerical system. p. 71.

Vol. 7, no. 1/2, 1956

MATEMATIKAI LAPOK

SCIENCE

HUNGARY

So: East European Accessions, Vol. 5, No. 9, Sept. 1956

TURAN, P.

Remark on the preceding paper of J. W. S. Cassels; application to approximative solution of algebraic equations. In English. p.291.  
(Acta Mathematica, Vol. 7, no. 3/4, 1956, Budapest, Hungary)

SO: Monthly List of East European Accessions (MEAL) IC. Vol. 6, No. 9, Sept. 1957. Uncl.

TURÁN, Paul.

Turán, Paul. Remark on the theory of quasianalytic function-classes. Magyar Tud. Akad. Mat. Kutató Int. Közl. 17 (1956), 481-487 (1957). (Hungarian and Russian summaries)

L'auteur considère la quasi-analyticité dans le sens du reviewer. Une classe de fonctions localement intégrables  $L$  est quasi-analytique ( $\alpha$ ) dans ce sens, si deux fonctions  $f_1(x)$  et  $f_2(x)$  de cette classe satisfaisant à la relation  $\liminf_{h \rightarrow 0} \exp(h^{-\alpha}) \int_{x-h}^{x+h} |f_1(x) - f_2(x)| dx < \infty$  sont nécessairement égales p.p. Il y a quelques années l'auteur [voir par ex. "Eine neue Methode in der Analysis und deren Anwendungen", Akadémiai Kiadó, Budapest, 1953; MR 15, 688] a pu, en utilisant ses méthodes d'évaluation du maximum d'un polynôme trigonométrique par son maximum sur un sous-intervalle, introduire un nouveau critère d'une telle quasi-analyticité. Tandis que le reviewer caractérise une telle quasi-analyticité par la "lacunarité" de la série de Fourier [Séries de Fourier et classes quasianalytiques, Gauthier-Villars, Paris, 1935], procédé généralisé par B. Ya. Levin pour les fonctions presque-périodiques [Doklady Akad. Nauk SSSR (N.S.) 65 (1949), 605-608; MR 11, 23], l'auteur caractérise la classe par

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Turan, Paul. Remark on the theory of Quasi-analytic function classes. 2

$$(1) \quad f(x) = \sum_1 a_j \exp(i t_j x),$$

$$(2) \quad \limsup_{\omega \rightarrow \infty} \exp(2\alpha^{-1} \omega \log \omega) \sum_{j \geq \omega} |a_j| < \infty.$$

L'auteur a démontré que si

$$(3) \quad \liminf_{h \rightarrow 0} \exp(h^{-\alpha}) \max_{x_1 - h \leq x \leq x_2} |f_1(x) - f_2(x)| < \infty,$$

$f_1$  et  $f_2$  appartenant à la classe, alors  $f_1 = f_2$  p.p. L'auteur cherche maintenant à démontrer que son résultat ne peut pas être beaucoup amélioré. Ainsi, la condition (2) ne peut pas être remplacée par la condition

$$(4) \quad \limsup_{\omega \rightarrow \infty} \exp(\omega^{1-\alpha}) \sum_{j \geq \omega} |a_j| < \infty.$$

En effet, en posant  $\beta = 2[1/\alpha] > \max(2, \alpha)$ ,  $\beta$  pair, la fonction  $f(x) = \exp(-1/\sin^\beta x)$ , tout en satisfaisant aux conditions (1), (4) et la relation  $\liminf_{h \rightarrow 0} \exp(h^{-\alpha}) \max |f(x)| < \infty$ , n'est pas identiquement nulle.

S. Mandelbrojt (Paris)

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1725:

Balázs, J.; and Turán, P. Notes on interpolation, III. Convergence. Acta Math. Acad. Sci. Hungar. 9 (1958), 195-214.

This investigation is a contribution to "lacunary" interpolation. If the interpolation points are  $x_\nu = x_{\nu n}$ ,  $\nu = 1, 2, \dots, n$ , we form the polynomials

$$R_n(x) = \sum_{\nu=1}^n \alpha_\nu r_\nu(x) + \sum_{\nu=1}^n \beta_\nu \rho_\nu(x)$$

of degree  $2n-1$  for which  $R_n(x_\nu) = \alpha_\nu$  and  $R_n''(x_\nu) = \beta_\nu$  are prescribed. The "fundamental polynomials"  $r_\nu(x)$ ,  $\rho_\nu(x)$  are uniquely determined. The authors investigate the particular case when the  $x_{\nu n}$  are the zeros of  $(1-x^2) \times P_{n-1}'(x)$ ,  $P_n$  Legendre's polynomial, and study the convergence of  $R_n(x)$ ,  $n \rightarrow \infty$ , associated with a given function  $f(x)$ ,  $\alpha_\nu = f(x_{\nu n})$ ,  $\beta_\nu$  given constants. The following two principal results are obtained. Let  $f'(x)$  be continuous with modulus  $\omega(\delta)$  such that  $\int_0^1 \omega(t) dt < \infty$ . Let  $n^{-1} \max_{(\nu)} |\beta_{\nu n}| \rightarrow 0$  as  $n \rightarrow \infty$ . Then  $R_n(x) \rightarrow f(x)$  uniformly in  $-1 \leq x \leq 1$ . Let  $0 < \epsilon < 1$  be given; there exists  $F(x) \in \text{Lip}(1-\epsilon)$  such that the associated polynomials  $R_n(x)$  (even for  $\beta_{\nu n} = 0$ ) are unbounded for  $x=0$ .

G. Szegő (Stanford, Calif.)

TURAN, P.; BALAZS, J.

Notes on interpolation. IV. Inequalities. p. 243.

ACTA MATHEMATICA. (Magyar Tudomanyos Akademia) Budapest, Hungary. Vol. 9,  
no. 3/4, 1958.

Monthly list of East European Accessions, (EEAI) LC, Vol. 9, No. 1, 1960.  
Uncl.

TURAN, P.; EGERVARY, E.

Notes on interpolation. V. On the stability of interpolation. p. 259.

ACTA MATHEMATICA. (Magyar Tudomanyos Akademia) Budapest, Hungary, Vol. 9,  
no. 3/4, 1958.

Monthly list of East European Accessions, (EEAI) LC, Vol. 9, no. 1, 1960.

Uncl.

TURAN, P.

A remark concerning the behavior of a power series on the periphery of its convergence circle, In English. p. 19.

Srpska akademija nauka. Matematički institut. PUBLICATIONS.  
Beograd, Yugoslavia. Vol. 12, 1958

Monthly list of East European Accessions (EEAI) LC, Vol, 8, no. 8, Aug., 1959.

Uncl.

TURAN, P.

16(1)

PHASE I BOOK EXPLOITATION

SOV/2660

Vsesoyuznyy matematicheskiy s'yezd. 3rd, Moscow, 1956  
Trudy. t. 4: Kratkoye soderzaniye sektsionnykh dokladov. Doklady  
Inostrannykh uchennykh (Transactions of the 3rd All-Union Mathema-  
tical Conference in Moscow. vol. 4: Summary of Sectional Reports.  
Reports of Foreign Scientists) Moscow, Izd-vo AN SSSR, 1959.  
247 p. 2,200 copies printed.

Sponsoring Agency: Akademiya nauk SSSR. Matematicheskiy Institut.

Tech. Ed.: G.M. Shevchenko; Editorial Board: A.A. Abramov, V.G.  
Boltyanskiy, A.M. Vasil'yev, B.V. Medvedev, A.D. Myshkis, S.M.  
Nikol'skiy (resp. Ed.), A.G. Postnikov, Yu. V. Prokhorov, K.K.  
Ruhlov, P. L. Ul'yanov, V.A. Uspenskiy, N.G. Chetaev, G. Ya.  
Shilov, and A.I. Shirshov.

PURPOSE: This book is intended for mathematicians and physicists.

COVERAGE: The book is Volume IV of the Transactions of the Third All-  
Union Mathematical Conference, held in June and July 1956. The  
book is divided into two main parts. The first part contains sum-  
maries of the papers presented by Soviet scientists at the Con-  
ference that were not included in the first two volumes. The  
second part contains the text of reports submitted to the editor  
by non-Soviet scientists. In those cases when the non-Soviet sci-  
entist did not submit a copy of his paper to the editor, the title  
of the paper is cited and, if the paper was printed in a previous  
volume, reference is made to the appropriate volume. The papers,  
both Soviet and non-Soviet, cover various topics in number theory,  
algebra, differential and integral equations, functional analysis,  
problems of mechanics and physics, computational mathematics,  
mathematical logic and the foundations of mathematics, and the  
history of mathematics.

Obreshkov, M. (Bulgaria). On one of the problems of Diophan- 133  
tine approximations of linear forms

Turan, P. (Hungary). On the completeness hypothesis in the 140  
theory of Riemann's zeta function

Rua, Lo-Keng (Chinese People's Republic). On the Turri pro- 140  
blem

Section on Algebra

Orrell, G. (German Democratic Republic). On the construction 144  
of rings in fields of algebraic numbers and functions

Card 25/34

TURAN, P.; REDEI, L.

Data on the theory of algebraic equations of finite bodies. p. 223.

ACTA ARITHMETICA. (Polska Akademia Nauk. Instytut Matematyczny) Warszawa, Poland. Vol. 5, no. 2, 1959

Monthly List of East European Accessions (EEAI) Lc, Vol. 9, no. 2, Feb. 1960

Uncl.

TURAY, Pal

Lipót Fejér (1880-1959); an obituary. *Magy.tud.* 66 no.12:653-654  
D '59. (EEAI 9:4)  
(Fejér, Lipót) (Mathematicians, Hungarian)

TURAN, P.

Lipót Fejér; obituary. Usp. mat. nauk 15 no.4:11-122 J1 Ag '60.  
(MIRA 13:9)

(Fejér, Lipót, 1880-1959)



ALPAR, Laszlo; TURAN, Pal

Data on the value distribution of an entire function. Mat kut kozl  
MTA 6 no.1/2:157-164 '61.

(Functions) (Distribution(Probability theory))

TURAN, Pal

On a density theorem of Yu.V.Linnik. Mat kut kozl MTA 6 no.1/2:  
165-179 '61.

(Linnik, Iurii Vladimirovich) (Functions)  
(Numbers, Theory of)

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A060/A000

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AUTHOR: Turán, P.

TITLE: A remark on Hermite-Fejér interpolation

PERIODICAL: Referativnyy zhurnal, Matematika, no. 11, 1962, 19, abstract 11B88  
(Ann. Univ. scient. budapest. Sec. math., 1960 - 1961, v. 3 - 4, 369  
- 377; English)

TEXT: The author considers the Hermite interpolation polynomial

$$H_n(f) = \sum_{v=1}^n f(x_{vn}) h_{vn}(x) + \sum_{v=1}^n y'_{vn} \xi_{vn}(x),$$

$$h_{vn}(x) = \left\{ 1 - \frac{\omega_n''(x_{vn})}{\omega_n'(x_{vn})} (x - x_{vn}) \right\} l_{vn}^2(x),$$

$$\xi_{vn}(x) = (x - x_{vn}) l_{vn}^2(x),$$

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A remark on Hermite-Fejér interpolation

$$l_{\nu n}(x) = \frac{\omega_n(x)}{\omega_n'(x_{\nu n})(x - x_{\nu n})}, \quad \omega_n(x) = \prod_{\nu=1}^n (x - x_{\nu n}),$$

$$(\nu = 1, 2, \dots, n; \quad n = 1, 2, \dots)$$

of the degree  $\leq 2n-1$ , where  $-1 \leq x_{nn} < \dots < x_{1n} \leq 1$ . As had been shown by L. Fejér, in the case of Chebyshev abscissae, we have  $\lim_{n \rightarrow \infty} H_n(f) = f(x)$  uniformly for

every function  $f(x) \in C[-1, +1]$  (i.e., continuous on  $[-1, +1]$ ), provided only  $y'_{\nu n} = o\left(\frac{n}{\lg n}\right)$ . The author investigates the behavior of the polynomial

$H_{\nu}^*(n), n(f)$  of degree  $\leq 2n - 2$ , coinciding with  $f(x)$  at the points  $x = \eta_1, \eta_2, \dots, \eta_n$ , where

$$\left\{ \frac{dH_{\nu}^*(n), n(f)}{dx} \right\}_{x=\eta_i} = y'_{in}$$

for  $1 \leq i \leq n$ , except for  $i = \nu(n)$ . In the case of Chebyshev abscissae, if for all  $n = 1, 2, \dots$  the exceptional point  $\eta_{\nu}(n)$  lies in the interval  $[-1 + \epsilon, 1 - \epsilon]$ ,

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A remark on Hermite-Fejér interpolation

$1 - \epsilon]$ ,  $0 < \epsilon \leq \frac{1}{4}$ , and if  $y'_{in} = 0$ ,  $1 \neq v(n)$ , then the condition

$$\int_{-1}^1 \frac{f(x) dx}{\sqrt{1-x^2}} = 0 \quad (1)$$

is necessary and sufficient for uniform convergence

$$\lim_{n \rightarrow \infty} H_{v(n), n}^*(f) = f(x), \quad -1 \leq x \leq +1, \quad f(x) \in C[-1, +1];$$

now, if the exceptional point lies sufficiently close to the point  $x_0 = \cos \frac{\pi}{5}$ , then the corresponding interpolation polynomials are uniformly bounded if, and only if, the function  $f(x)$  is bounded on  $[-1, +1]$ , where it is always possible to choose a function  $f_1(x) \in C$ , for which the limit  $\lim_{n \rightarrow \infty} H_{v(n), n}^*(f)$  does not exist at the point  $x_0$ . If the points are roots of the polynomial  $\int_{-1}^x P_{n-1}(t) dt$ , where  $P_{n-1}(t)$  is a Legendre polynomial normed by the condition  $P_{n-1}(1) = 1$ , then under the same conditions relative to the exceptional point we have instead

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A remark on Hermite-Fejér interpolation

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of (1) the condition  $f(-1) = f(+1)$  as the necessary and sufficient condition  
for the uniform convergence of  $\lim_{n \rightarrow \infty} H_n^*(f) = f(x)$  on the interval  
 $[-1 + \delta, 1 - \delta]$ ,  $0 < \delta \leq \frac{1}{2}$  for  $f(x) \in C$ .

Ya.L. Geronimus

[Abstracter's note: Complete translation]

Card 4/4

ERDOS, P. (Budapest); TURAN, P., acad. (Budapest)

An extremal problem in the theory of interpolation. Acta mat Hung  
12 no.1/2:221-234 '61. (EAI 10:9)

1. Corresponding member of the Hungarian Academy of Sciences (for  
Erdos). 2. Hungarian Academy of Sciences (for Turan).

(Interpolation) (Polynomials)

HAJOS, Gyorgy; KALMAR, Laszlo; SURANYI, Janos; TURAN, Pal; FOSA, Lajos;  
DE BRUJIN, N.G. (Amsterdam, Holland); SARKADI, Karoly; FRIED,  
Ervin; WIEGANDT, Richard; ERDOS, Pal

Mathematical problems. Mat lapok 12 no.3/4:253-258 '61.

1. "Matematikai Lapok" szerkesztoje (for Hajos and Kalmar).
2. "Matematikai Lapok" felelos szerkesztoje (for Turan).



TURAN, Pal, Member of the Hungarian Academy of Sciences

On some further one-sided theorems of new type in the theory of diophantine approximations. Acta mat Hung 12 no.3/4:455-468 '61.

1. Editorial Board Member, "Acta Mathematica Academiae Scientiarum Hungaricae."

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A060/A000

16.6500

AUTHOR: Balázs, J., Turán, P.

TITLE: Notes on interpolation. VIII (Mean convergence in infinite intervals)

PERIODICAL: Referativnyy zhurnal, Matematika, no. 11, 1962, 19 - 20, abstract 11B89 (Acta math. Acad. scient. hung., 1961, v. 12, no. 3 - 4, 469 - 474; English; summary in Russian)

TEXT: For part VII see RZhMat, 1960, 5130. Say a triangular matrix of interpolation points  $A = \|x_{kn}\|$ ,  $k = 1, 2, \dots, n$ ;  $n = 1, 2, 3, \dots$  is composed of the roots  $x_{kn}$  ( $k = 1, 2, \dots, n$ ) of the orthogonal polynomials  $q_n(x)$  ( $n = 1, 2, 3, \dots$ ) corresponding to some differential weight  $p(x)$  on the infinite interval  $(-\infty, +\infty)$ , so that  $\int_{-\infty}^{+\infty} q_m(x) q_n(x) p(x) dx = 0$  for  $m \neq n$ . For the points  $x_{kn}$  situated in every column of the matrix  $A$ , a Lagrange interpolation polynomial  $L_n(f, x)$  of the function  $f(x)$  is constructed. It is required to find the conditions under which the sequence of interpolation polynomials  $L_n(f, x)$  converges "in the mean" to the function  $f(x)$ , i.e.,

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Notes on interpolation. VIII ....

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$$\int_{-\infty}^{+\infty} \{f(x) - L_n(f, x)\}^2 p(x) dx \rightarrow 0$$

for  $n \rightarrow \infty$ . Theorem: Let the differential weight  $p(x)$  satisfy the following conditions:  $p(x) = \frac{h(x)}{g(x)}$ , where the function  $h(x) \geq 0$  and is integrable on the entire  $x$  axis, and the function  $g(x)$  is even and has derivatives of all orders, where  $g^{(2v)}(x) > 0$ ,  $v = 0, 1, 2, \dots$ , for any  $x$ ; moreover, for  $x > 0$  the function  $\ln g(x)$  is a convex function of  $\ln x$  and

$$\int_0^{+\infty} \frac{\ln g(x)}{x^2} dx = +\infty.$$

If the function  $f(x)$  is continuous on the entire axis, and

$$\lim_{x \rightarrow \pm\infty} \frac{f(x)}{\sqrt{g(x)}} = 0, \text{ then } \lim_{n \rightarrow \infty} \int_{-\infty}^{+\infty} \{f(x) - L_n(f, x)\}^2 p(x) dx = 0.$$

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Corrolary: If the matrix A is composed of the roots of the Hermite polynomials  $H_n(x)$ , then for every function  $f(x)$  continuous on the whole axis, and satisfying

$$\lim_{x \rightarrow \pm\infty} f(x) e^{-\left(\frac{1}{2} - \epsilon\right) x^2} = 0$$

(where  $\epsilon > 0$  is an arbitrarily small number), the condition

$$\lim_{n \rightarrow \infty} \int_{-\infty}^{+\infty} \{f(x) - L_n(f, x)\}^2 e^{-x^2} dx = 0$$

is fulfilled.

V.F. Nikolayev

[Abstracter's note: Complete translation]

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